

YEAR 6

Efficient Methods

Worked examples for Key Stage 2

ARITHMETIC

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- ⑱ $(-)$ \rightarrow i \rightarrow $\frac{\times}{\div}$ \rightarrow $\frac{+}{-}$
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- ㉚ + - fractions
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① $5682 + 379$

$$\begin{array}{r} 5682 \\ + 379 \\ \hline 6061 \end{array}$$

← be sure to line up
by place value

↑ your answer does not
need commas

② $6807 - 394$

$$\begin{array}{r} 6807 \\ - 394 \\ \hline 6413 \end{array}$$

only exchange if
needed

③ $4000 - 3947$

$$\begin{array}{r} 4000 \\ - 3947 \\ \hline 0053 \end{array}$$

← make sure you don't
exchange here

Your answer is 53, not 0053.

④

$$\begin{array}{r} 52 \\ 684 \\ \times 6 \\ \hline 4104 \end{array}$$

← don't forget to add
these on.

⑤

$$\begin{array}{r} + \quad + \quad + \\ 3 \quad 2 \quad 4 \quad 6 \\ \times \quad \quad \quad \quad 4 \quad 5 \\ \hline 1 \quad 6 \quad 2 \quad 3 \quad 0 \end{array}$$

← cross out after you've used these

add ↑

$$\begin{array}{r} + \\ 1 \quad 2 \quad 9 \quad 8 \quad 4 \quad 0 \\ \hline 1 \quad 4 \quad 6 \quad 0 \quad 7 \quad 0 \end{array}$$

← this row, times each by 5
← this row, times each by 4.
don't forget the place holder

⑥

$$\begin{array}{r} \quad \quad \quad \times 100 \quad \quad \quad \times 10 \\ 3 \quad 4 \quad \checkmark \quad \checkmark \quad \times \quad 2 \quad \checkmark = 6 \quad 8 \quad \checkmark \quad \checkmark \quad \checkmark \\ 3 \quad 4 \quad \times \quad 2 = 6 \quad 8 \end{array}$$

then 100x bigger and 10x bigger

$$\begin{array}{r} \checkmark \quad \checkmark \quad \checkmark \quad \quad \quad \checkmark \quad \checkmark \\ 6 \quad 0 \quad 0 \quad 0 \quad \times \quad 4 \quad 0 \quad 0 = 2 \quad 4 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \\ 6 \quad \times \quad 4 = 2 \quad 4 \end{array}$$

then 1000x bigger then 100x bigger

Mental

⑦

$$\begin{array}{r} 3 \quad 6 \quad 0 \quad 0 \div 1 \quad 2 \\ \hline 3 \quad 6 \quad \checkmark \quad \checkmark = 3 \quad 0 \quad 0 \\ 1 \quad 2 \end{array}$$

← 36 ÷ 12

Mental

$$\begin{array}{r} 4 \quad 0 \quad 0 \quad 0 \div 8 \quad 0 \\ \hline 4 \quad 0 \quad \emptyset \quad \checkmark = 5 \quad 0 \\ 8 \quad \emptyset \end{array}$$

← cancel pairs of zeroes.
↓ 40 ÷ 8

$$\begin{array}{r} 2 \quad 5 \quad 0 \div 5 \quad 0 \\ \hline 2 \quad 5 \quad \emptyset = 5 \\ 5 \quad \emptyset \end{array}$$

← 25 ÷ 5

8
M
e
n
t
a
l

When \div or \times by 10, 100 or 1000

use the grids and "jump"
smaller $\xrightarrow{\div}$ $\xleftarrow{\times}$ larger

$45 \div 10 = 4.5$ $\div 10$ (one jump)

$\div 100$ (2 jumps)

$\div 1000$ (3 jumps)

45
 4.5

Whole numbers have decimals and the end.

$8.3 \times 100 = 830$

$$\begin{array}{r} 8.3 \\ 83. \\ 830. \end{array}$$

9

$7248 \div 5 = 1449 \text{ r } 3$

$1449 \text{ r } 3$ \leftarrow on SATs Test 1,

$5 \overline{) 7248}$

Leave the remainder

Check by doing the unverse:

$$\begin{array}{r} 2 2 4 \\ 1449 \\ \times 5 \\ \hline \end{array}$$

7245 then add the 3 remainder
 $+ 3$

7248 \leftarrow this is the same

(Short division)

⑩ $8022 \div 21$

$$\begin{array}{r} 382 \\ 21 \overline{) 8022} \end{array}$$

↑ list 1st, 2nd, 4th, 8th multiple of 21 to start

(21 goes into 80 3 times)
($80 - 63 = 17$)
↑
remainder

- ① 21
- ② 42
- ④ 84

I needed
↓ this

$$\begin{array}{r} 21 \\ \times 3 \\ \hline 63 \end{array} \textcircled{3}$$

(21 goes into 172 6 times)
($172 - 168 = 4$)
↑
remainder

- ⑧ 168

$$\begin{array}{r} 21 \\ \times 7 \\ \hline 147 \end{array} \textcircled{7}$$

(21 goes into 42 2 times)
($42 - 42 = 0$)

On SATs Paper 1, these usually don't have remainders.

Check by doing 21×382 .

$$\begin{array}{r} 382 \\ \times 21 \\ \hline 7640 \\ \hline 8022 \checkmark \end{array}$$

(Short division)

⑩ 8022 ÷ 21

382
21 | 8022

list 1st, 2nd, 4th, 8th
multiple of 21
to start

(21 goes into 80 3 times)
(80 - 63 = 17)
↑
remainder

- ① 21
- ② 42
- ④ 84
- ⑧ 168

I needed
↓ this
21

x 3
63 ③

(21 goes into 172 8 times)
(172 - 168 = 4)
↑
remainder

21
x 7
147 ⑦

(21 goes into 42 2 times)
(42 - 42 = 0)

On SATs Paper, these usually don't
have remainders.

Check by doing 21 x 382.

382
x 21

7640

8022 ✓

(11) $362.4 + 8.99$

$$\begin{array}{r} 362.40 \\ + 8.99 \\ \hline 371.39 \end{array}$$

← add place holders
← ensure you line up by place value

Don't forget →
in your answer ↑

Your decimals should be in a line

(12) $382.6 - 1.43$

↑
must be on top

$$\begin{array}{r} 382.60 \\ - 1.43 \\ \hline 381.17 \end{array}$$

you must have place holders.
↓
← Exchange
← line up by place value

$$35 - 0.82$$

$$\begin{array}{r} 35.00 \\ - 0.82 \\ \hline 34.18 \end{array}$$

← Whole numbers have decimals at the end.
Remember to add place holders and exchange.

Check with addition

$$\begin{array}{r} 34.18 \\ + 0.82 \\ \hline 35.00 \checkmark \end{array}$$

⑬

$$5032 - ? = 479$$

5032
? 479

$$\leftarrow 5032 - 479$$

$$\begin{array}{r} 4 \overset{9}{\cancel{10}} \overset{12}{\cancel{3}} \overset{12}{\cancel{2}} \\ - 479 \\ \hline 4553 \end{array}$$

$$? = 4553$$

Check :

$$\begin{array}{r} 4 \overset{9}{\cancel{10}} \overset{12}{\cancel{3}} \overset{12}{\cancel{2}} \\ - 4553 \\ \hline 479 \checkmark \end{array}$$

$$? + 824 = 1063$$

1063
? 824

$$\begin{array}{r} 1063 - 824 \\ 0 \overset{10}{\cancel{10}} \overset{13}{\cancel{5}} \overset{13}{\cancel{3}} \\ - 824 \\ \hline 239 \end{array}$$

$$? = 239$$

Check :

$$\begin{array}{r} 2 \overset{1}{\cancel{3}} \overset{1}{\cancel{9}} \\ + 824 \\ \hline 1063 \checkmark \end{array}$$

14

M
e
n
t
a
l

$$0.\overset{\textcircled{1}\text{dp}}{4} \times 5 = 2.\overset{\textcircled{1}\text{dp}}{0} \text{ which is } 2$$

$$4 \times 5 \text{ then } 1 \text{ dp } (\div 10)$$

$$\begin{array}{r} 20 \\ \hline \end{array}$$

$$3.\overset{\textcircled{1}\text{dp}}{6} \times 4 = 14.\overset{\textcircled{1}\text{dp}}{4}$$

$$36 \times 4 \text{ then } 1 \text{ dp } (\div 10)$$

$$\begin{array}{r} 144 \\ \hline \end{array}$$

$$0.\overset{\textcircled{1}\text{dp}}{0}\overset{\textcircled{2}\text{dp}}{8} \times 7 = 0.\overset{\textcircled{1}\text{dp}}{5}\overset{\textcircled{2}\text{dp}}{2}$$

$$8 \times 7 \text{ then } 2 \text{ dp } (\div 100)$$

$$\begin{array}{r} 56 \\ \hline 21 \end{array}$$

$$\begin{array}{r} 36 \\ \times 4 \\ \hline 144 \end{array}$$

15

$$\begin{array}{r} 4.63 \\ \times 5 \\ \hline 23.15 \end{array}$$

Do not line up decimals.
It stays in the same place when only one number has a decimal

$$\begin{array}{r} 8.2 \\ \times 5 \\ \hline 41.0 \end{array} \text{ which is } 41.$$

16

$$0.\overset{\textcircled{1}\text{dp}}{8} \times 0.\overset{\textcircled{2}\text{dp}}{9} = 0.72$$

($\div 10$)

($\div 10$)

$$8 \times 9 = 72$$

then 2dp or $\div 10$ then $\div 10$

* These usually do not come up on the test.

① 38.6 ÷ 2 = 19.3

$$\begin{array}{r} 19.3 \\ 2 \overline{) 38.6} \end{array}$$

↖ The decimal goes straight up

35.6 ÷ 4 = 8.15

$$\begin{array}{r} 08.15 \\ 4 \overline{) 35.6} \end{array}$$

↖ Add zeroes and continue dividing. Remember that you can't have a remainder with a decimal.

① 8 ()

i²

X ÷ (whichever is first)

+ - (whichever is first)

3² = 3 × 3 = 9

4³ = 4 × 4 × 4 = 64

6 - 3 ÷ 1 × 2 + 4² - (2 + 1)

6 - 3 ÷ 1 × 2 + 4² - 3

6 - ~~3~~ ÷ ~~1~~ × 2 + 16 - 3

6 - ~~3~~ × 2 + 16 - 3

~~6~~ - ~~6~~ + 16 - 3

~~0~~ + ~~16~~ - 3

16 - 3

13

(19) $3\frac{1}{5}$ as an improper fraction:
 $5 \times 3 + 1$ (numerator)
 5 (denominator)

$$3\frac{1}{5} = \frac{16}{5}$$

$\frac{9}{5}$ as a mixed number

↑ how many fives into 9? 1

4 left over (numerator)
5 (denominator)

↑
whole
number

$$\frac{9}{5} = 1\frac{4}{5}$$

(20) $\frac{3}{5}$ of 40 = 24

$$40 \div 5 = 8 \quad \left(\frac{1}{5}\right)$$
$$8 \times 3 = 24 \quad \left(\frac{3}{5}\right)$$

↑
answer

of

$$\frac{4}{7} \times 28 = 16$$

$$28 \div 7 = 4 \quad \left(\frac{1}{7}\right)$$

$$4 \times 4 = 16 \quad \left(\frac{4}{7}\right) \leftarrow \text{answer}$$

21 Simplifying fractions:

$$\frac{7}{21}$$

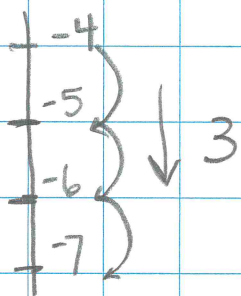
What goes into 7 and 21 evenly?

$$\frac{7 \div 7}{21 \div 7} = \frac{1}{3} \leftarrow \text{simplified}$$

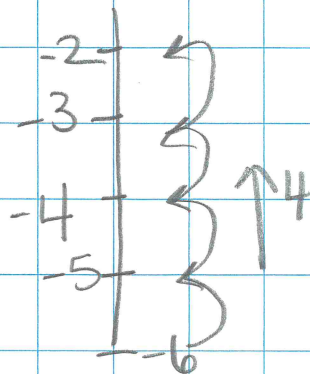
$$\frac{16 \div 2}{34 \div 2} = \frac{8}{17}$$

$$\frac{25 \div 5}{100 \div 5} = \frac{5 \div 5}{20 \div 5} = \frac{1}{4} \leftarrow \text{simplified}$$

22 $-4 - 3 = -7$



$$-6 + 4 = -2$$



$$-2 + -5 = -7$$

2 negatives add
5 negatives is
7 negatives

②③ To write a decimal as a percentage, write as a fraction first.

$$0.4 = \frac{4}{10} \stackrel{\times 10}{=} \frac{40}{100} = 40\%$$

↑ for a %

$$0.23 = \frac{23}{100} = 23\%$$

$$\frac{5}{20} \stackrel{\times 4}{=} \frac{20}{100} = 0.20 = 20\%$$

Decimals have denominators of 10, 100 or 1000. Percentages have denominators of 100. (powers of 10)

②④ Common equivalences.

$$\frac{1}{4} = 0.25 = 25\%$$

$$\frac{1}{5} = \frac{2}{10} = 0.2 = 20\%$$

$$\frac{1}{2} = 0.5 = 50\%$$

$$\frac{3}{4} = 0.75 = 75\%$$

25) $20\% \times 350$ is the same as
 20% of 350

$$20\% \text{ of } 350 = 70$$

$$\begin{array}{l} 100\% \rightarrow 350 \\ \xrightarrow{\div 10} 10\% \rightarrow 35 \\ \xrightarrow{\times 2} 20\% \rightarrow 70 \end{array}$$

Find 10% by
dividing by 10

↑ answer

$$\begin{array}{r} 350 \\ 35 \end{array}$$

OR

$$10\% + 10\% = 20\%$$

$$35 + 35 = 70$$

$$43\% \text{ of } 800 = 344$$

$$\begin{array}{l} 100\% \rightarrow 800 \\ \xrightarrow{\div 10} 10\% \rightarrow 80 \\ \xrightarrow{\div 10} 1\% \rightarrow 8 \end{array}$$

$$10\% + 10\% + 10\% + 10\% = 40\%$$

$$80 + 80 + 80 + 80 = 320$$

$$1\% + 1\% + 1\% = 3\%$$

$$8 + 8 + 8 = 24$$

$$40\% + 3\% = 43\%$$

$$320 + 24 = 344$$

Other %

Find 5% by halving 10%.

Find 50% by halving the whole.

Find 25% by finding a quarter of the whole.

②6 To multiply fractions, you don't need common denominators:

$$\frac{3}{5} \times \frac{2}{3} = \frac{6}{15} \quad \text{multiply straight across}$$

$$\frac{6 \div 3}{15 \div 3} = \frac{2}{5} \quad (\text{simplified})$$

②7 When \times by a whole, only multiply the tops.

$$\cancel{3} \times \frac{2}{3} = \frac{6}{3} = 2$$

$$4 \times \frac{2}{5} = \frac{8}{5} = 1\frac{3}{5}$$

②8 Partition when multiplying by a mixed number.

$$4\frac{2}{3} \times 7 = 32\frac{2}{3}$$

$$4 \times 7 = 28$$

$$\frac{2}{3} \times 7 = \frac{14}{3} = 4\frac{2}{3} \quad (\text{only } \times \text{ the top})$$

*Can't leave it like this

$$28 + 4\frac{2}{3} = 32\frac{2}{3}$$

2 8) Option 2 for multiplying
by a mixed number

$$4\frac{2}{3} \times 7$$

↓

Change to an improper fraction

$$\frac{14}{3} \times 7 = \frac{98}{3} = 32\frac{2}{3}$$

↑ Change back
to a mixed
number

Simplify if needed.

29) For \div , you do not need common denominators.

Change - to \times

$$\frac{3}{5} \div 2$$

← put "one over" and "x"

$$\frac{3}{5} \times \frac{1}{2} = \frac{3}{10}$$

(This is the same as $\frac{1}{2}$ of $\frac{3}{5}$)

30) Find common denominators when adding and subtracting

$$\frac{4}{5} + \frac{2}{3} = 1 \frac{7}{15}$$

$$\frac{4}{5} = \frac{8}{10} = \frac{12}{15}$$

$$\frac{2}{3} = \frac{4}{6} = \frac{6}{9} = \frac{8}{12} = \frac{10}{15}$$

$$\frac{12}{15} + \frac{10}{15} = \frac{22}{15} = 1 \frac{7}{15}$$

$$\frac{2}{3} - \frac{1}{4} = \frac{5}{12}$$

$$\frac{2}{3} = \frac{4}{6} = \frac{6}{9} = \frac{8}{12}$$

$$\frac{1}{4} = \frac{2}{8} = \frac{3}{12}$$

$$\frac{8}{12} - \frac{3}{12} = \frac{5}{12}$$

Be sure not to swap the order

31 When adding mixed numbers, remember to make sure you convert where needed.

EX: $3\frac{8}{3}$ can't be the answer because $\frac{8}{3}$ is improper

$$\begin{array}{c} 3 \\ \uparrow \\ 3 \end{array} + \begin{array}{c} 2\frac{8}{3} \\ \uparrow \\ 2 \end{array} = 6\frac{2}{3}$$

$$4\frac{4}{5} + 3\frac{3}{10} = 8\frac{1}{10}$$

$$4\frac{4}{5} = 4\frac{8}{10}$$

$$3\frac{3}{10}$$

$$4\frac{8}{10} + 3\frac{3}{10} = 7\frac{11}{10}$$

$$7 + 1\frac{1}{10} = 8\frac{1}{10}$$

③② Subtracting mixed numbers when exchanging is not needed:

$$3\frac{2}{3} - 1\frac{1}{6}$$

$$3\frac{2}{3} = 3\frac{4}{6}$$

$$1\frac{1}{6}$$

You cannot switch
the fraction and
whole number

$$3\frac{4}{6} - 1\frac{1}{6} = 2\frac{3}{6} = 2\frac{1}{2} \text{ (simplified)}$$



Don't swap the order

③③ Subtracting mixed numbers when exchanging is needed:

$$4\frac{1}{4} - 2\frac{3}{4}$$

(denominators are
already the same)

$$\star 4\frac{1}{4} - 2\frac{3}{4} \neq 2\frac{2}{4} \star$$

not

$$3\frac{4}{4} - 2\frac{3}{4}$$

$$3\frac{5}{4} - 2\frac{3}{4} = 1\frac{2}{4} = 1\frac{1}{2} \text{ (simplified)}$$